

Package of Research Projects **"Diffusion in Zeolites"**

by CNRS (France), DFG (Germany), EPSRC (United Kingdom), NSF (USA)

Extension for the Period from 2006-2009

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## **Project 5**

# **Studying Zeolitic Diffusion by Interference and IR Microscopy**

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Sergey Vasenkov (Gainesville, University of Florida)

Pavel Kortunov (Exxon-Mobil)

Christian Chmelik

DB Shah (Cleveland University)

Lars Heinke

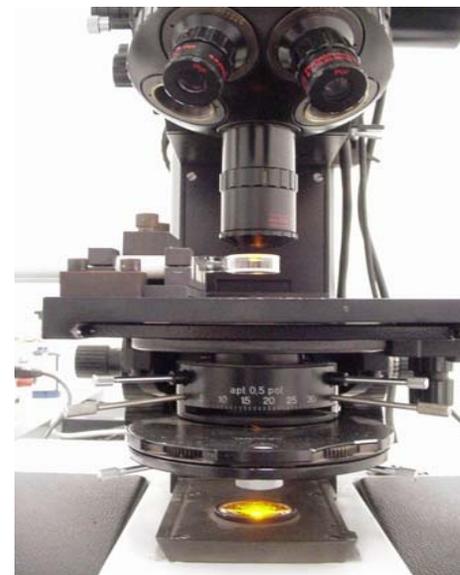
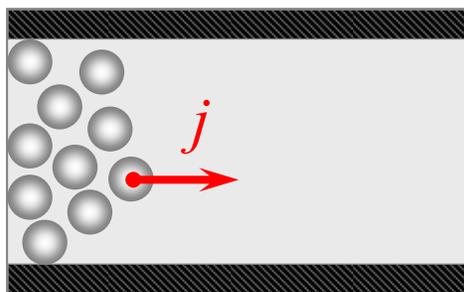
Despina Tzoulaki

# What do we measure?

## Interference Microscopy (IFM)

$$j = -D_{(T)} \text{grad } c$$

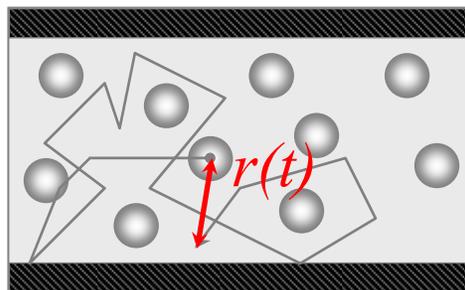
transport diffusion



## Pulsed Field Gradient (PFG) NMR

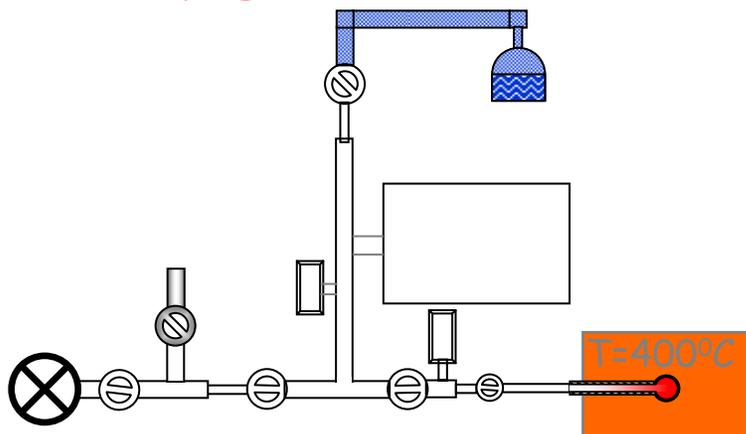
$$\langle r^2(t) \rangle = 2D t$$

self-diffusion

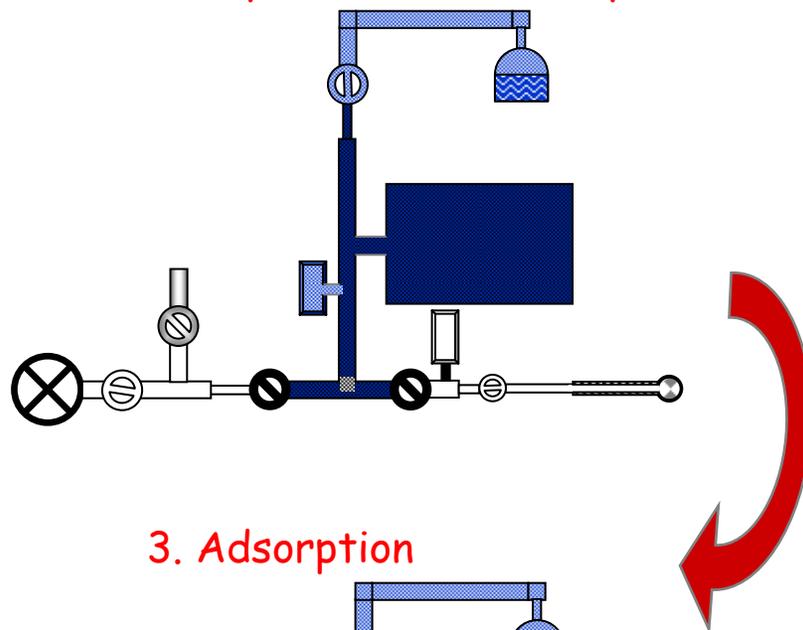


# Adsorption system and cycles

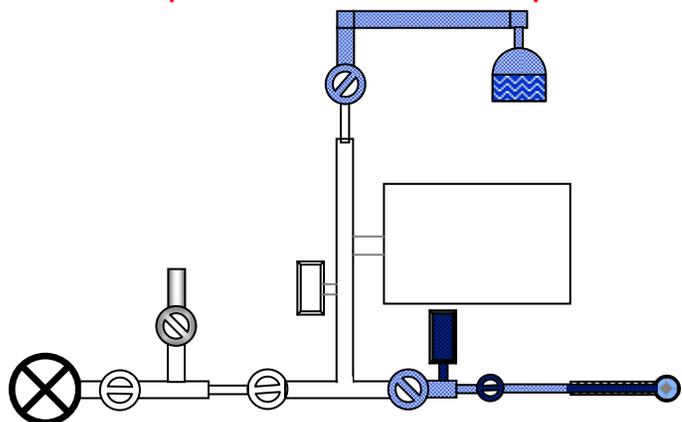
1. Pumping / Activation



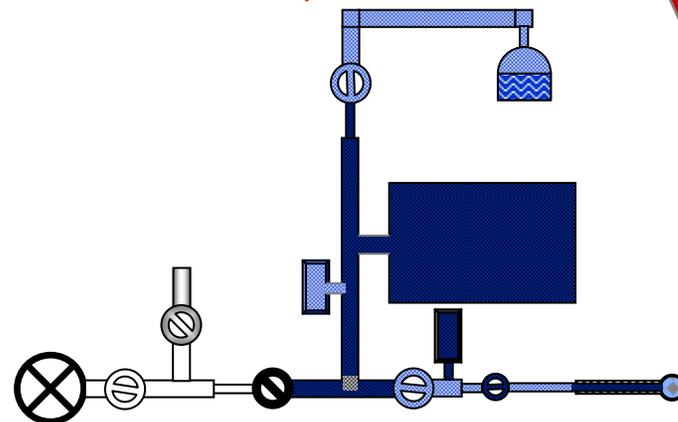
2. Preparation for adsorption



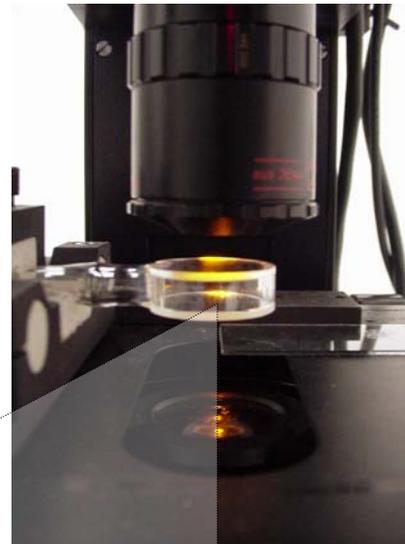
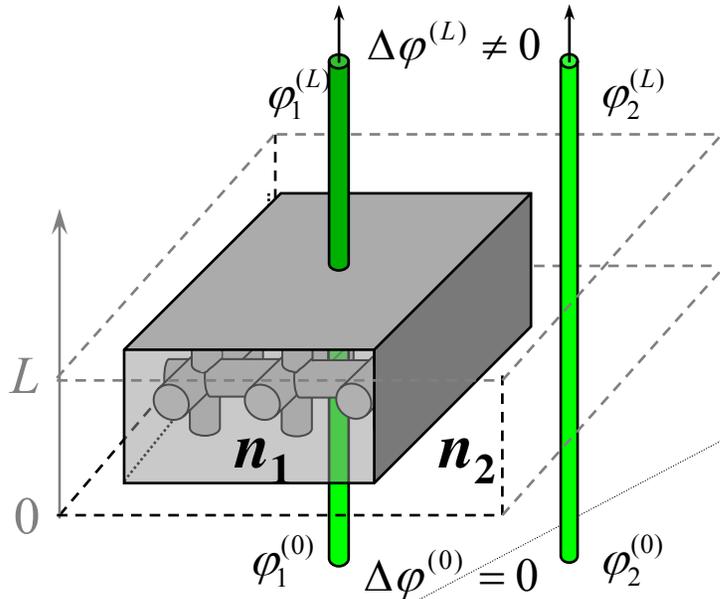
4. Preparation for desorption



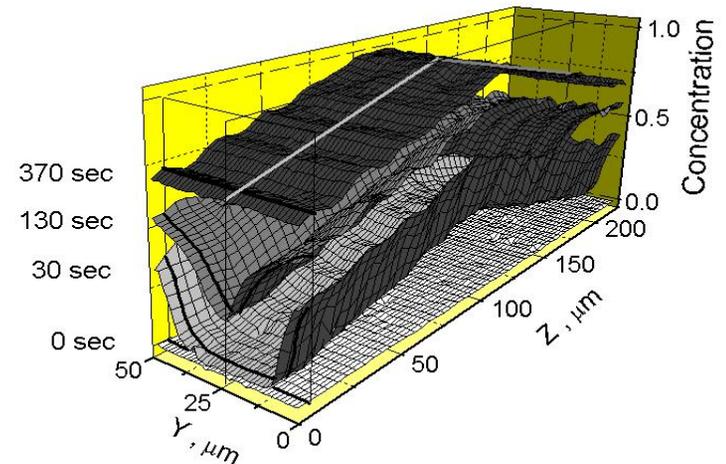
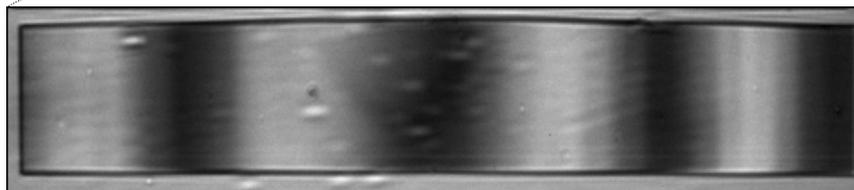
3. Adsorption



# IFM Technique



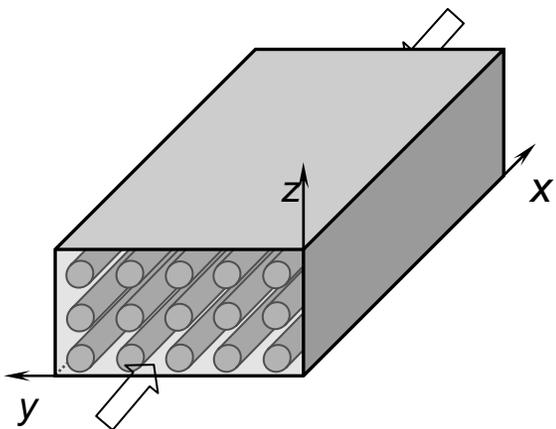
$$\Delta\varphi \sim \Delta n \sim \Delta c$$



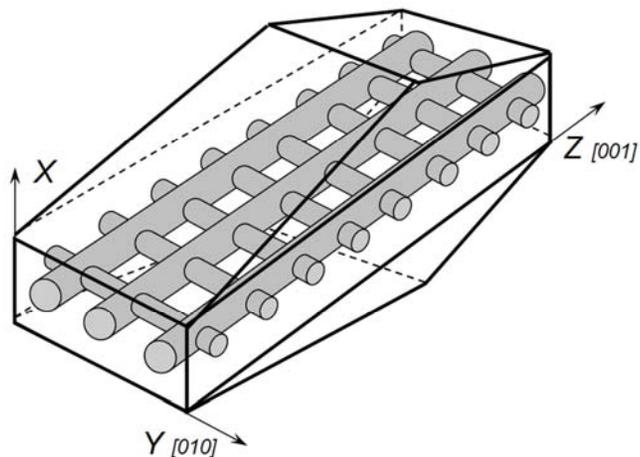
Spatial resolution:  $0.5 \mu\text{m} \times 0.5 \mu\text{m}$

# Outline

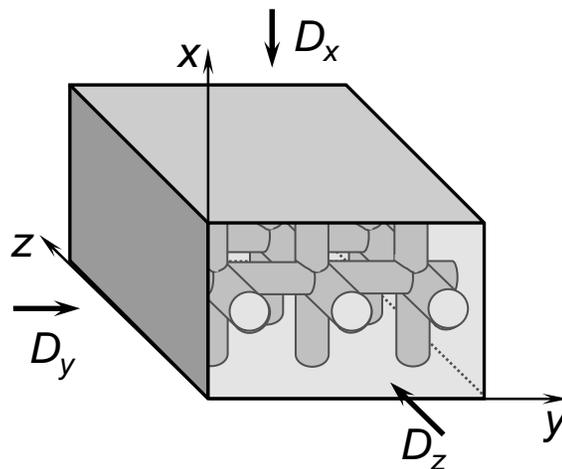
(a) 1-D pore structure of the MOF crystals



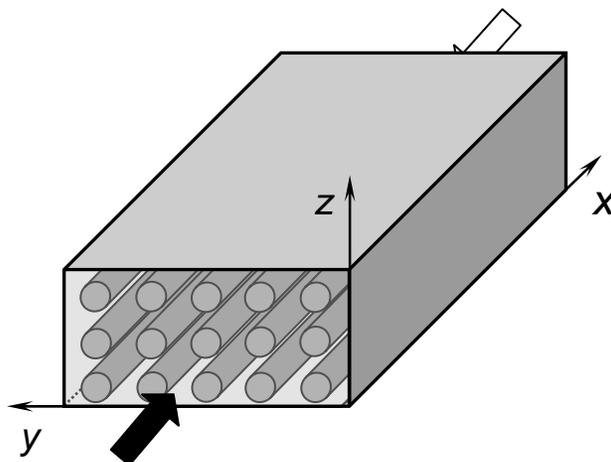
(b) 2-D pore structure of the Ferrierite zeolite



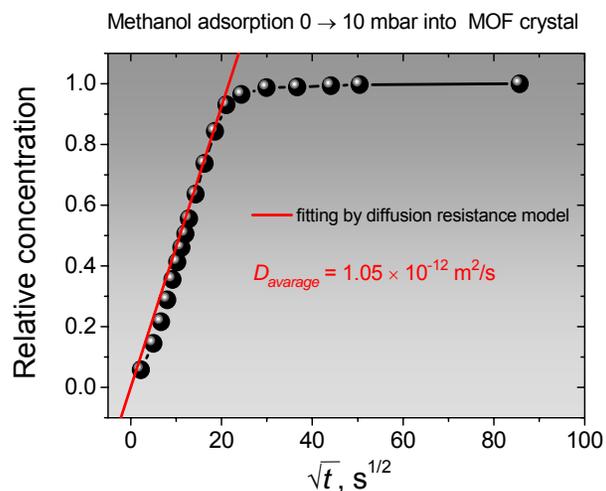
(c) 3-D pore structure of the SAPO STA-7



## 1-D pore structure of MOF crystal (\*)

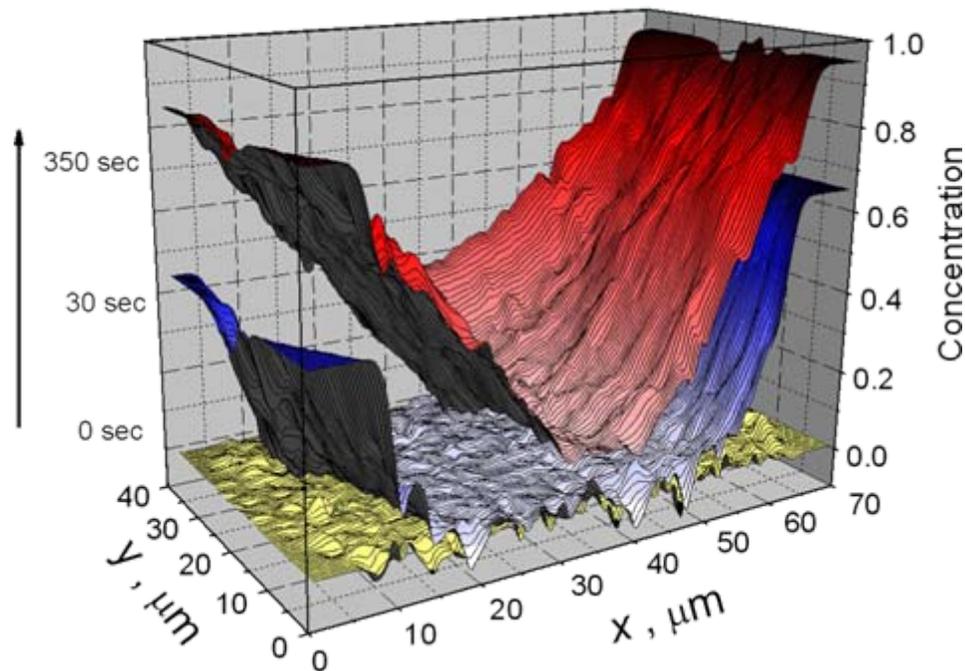


### Macroscopic adsorption techniques:



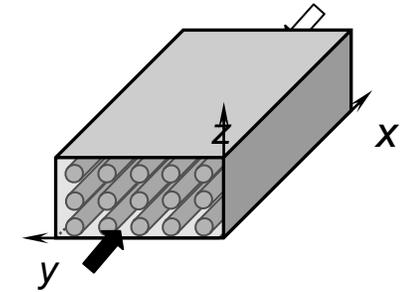
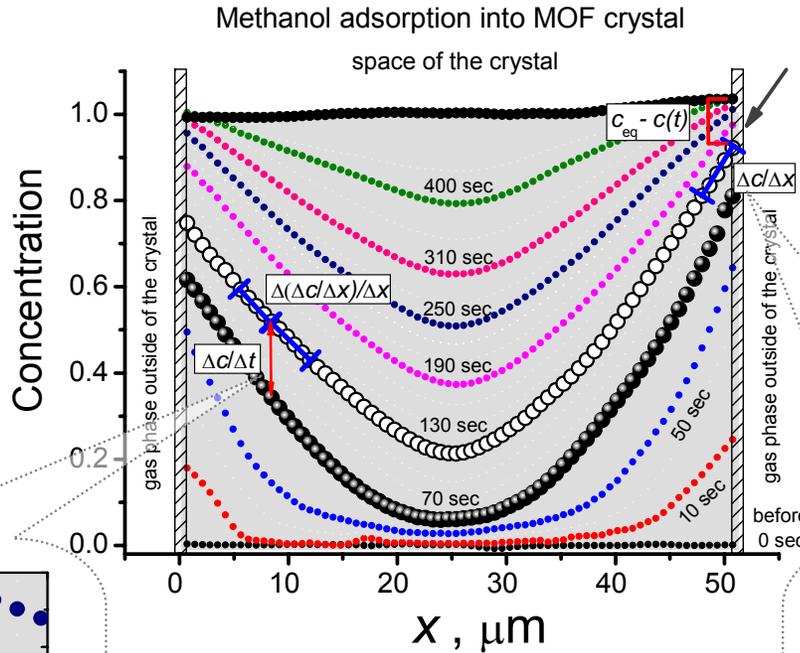
### Interference microscopy technique:

adsorption of Methanol (0 → 5 mbar) into MOF crystal



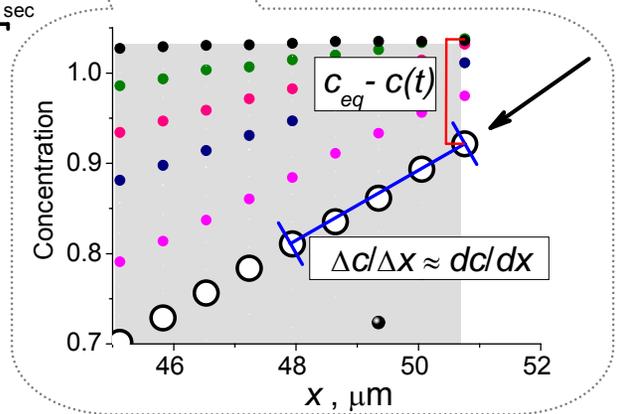
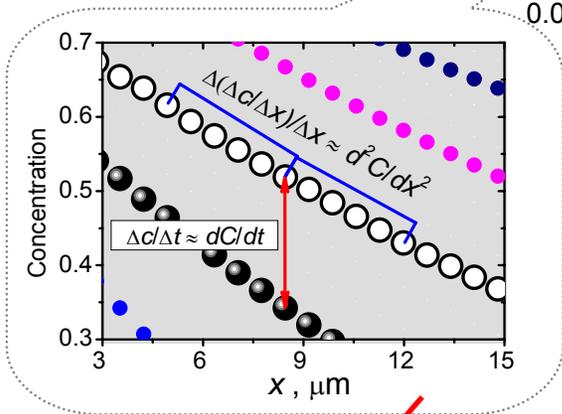
(\*) D.N. Dybtsev, H. Chun, S.H. Yoon, D. Kim and K. Kim; *J. Am. Chem. Soc.*, 2004, 126, 32-33

# First and second Fick's laws



**Local DIFFUSION**

**Surface PERMEABILITY**



$$\frac{\partial c}{\partial t} = \frac{\partial}{\partial x} \left[ D(c, x) \frac{\partial c}{\partial x} \right] = D(c, x) \frac{\partial^2 c}{\partial x^2} + \frac{\partial D(c, x)}{\partial c} \cdot \left( \frac{\partial c}{\partial x} \right)^2$$

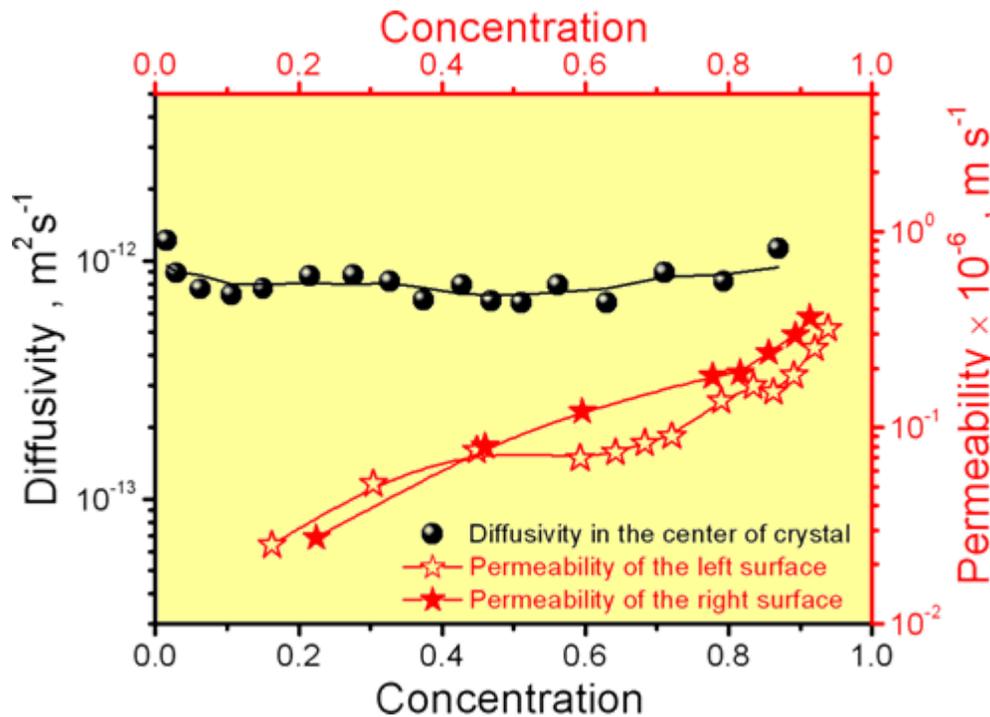
$$j = \alpha (c_{eq} - c(t)) = D(c(t)) \cdot \frac{dc}{dx}$$

# 1-D diffusion in the MOF crystal

## Local DIFFUSION

(microscopic analysis)

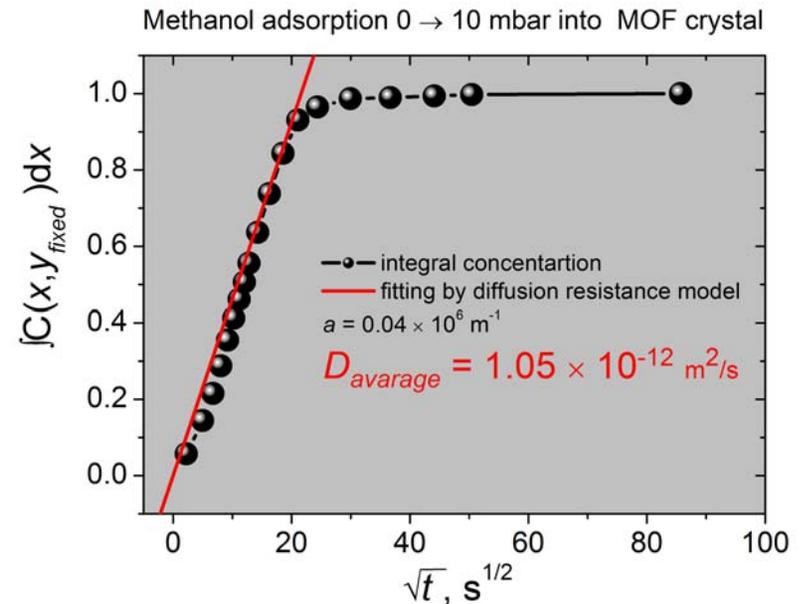
$$\frac{\partial c}{\partial t} = \frac{\partial}{\partial x} \left[ D(c, x) \frac{\partial c}{\partial x} \right] = D(c, x) \frac{\partial^2 c}{\partial x^2} + \frac{\partial D(c, x)}{\partial c} \cdot \left( \frac{\partial c}{\partial x} \right)^2$$



## Average DIFFUSION

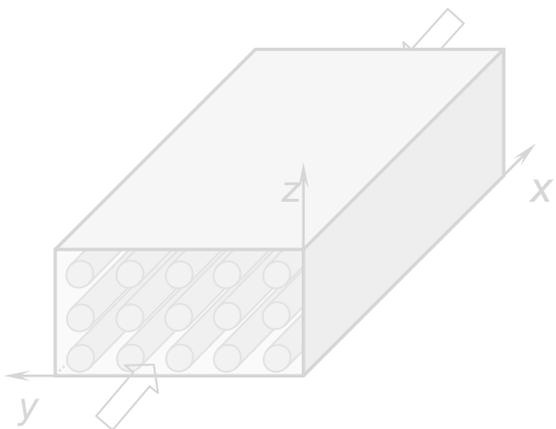
(macroscopic analysis)

$$\frac{c_t - c_0}{c_\infty - c_0} \approx 2a \sqrt{\frac{Dt}{\pi}}$$

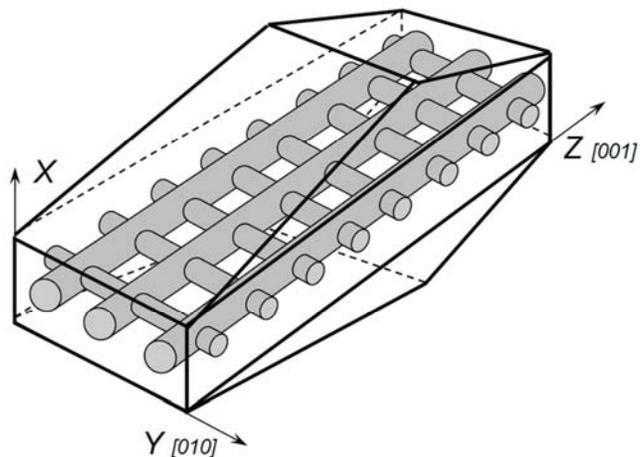


# Outline

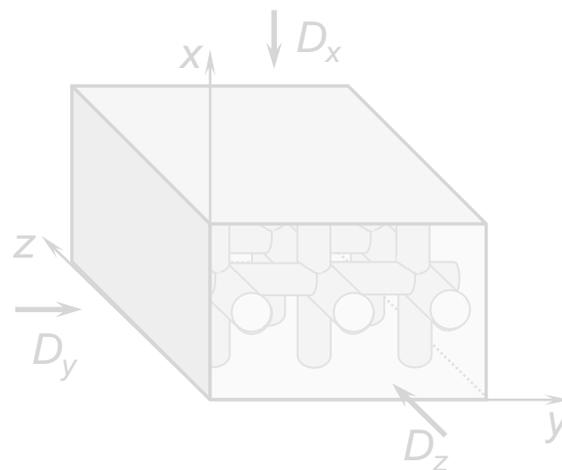
(a) 1-D pore structure of the MOF crystals



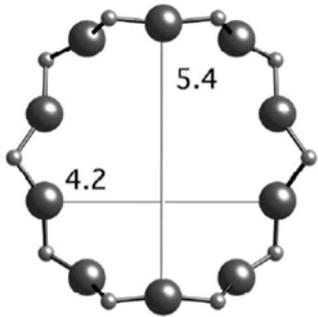
(b) 2-D pore structure of the Ferrierite zeolite



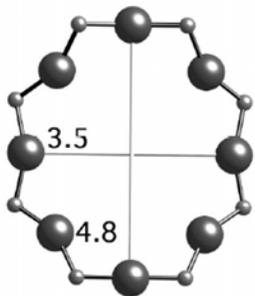
(c) 3-D pore structure of the SAPO STA-7



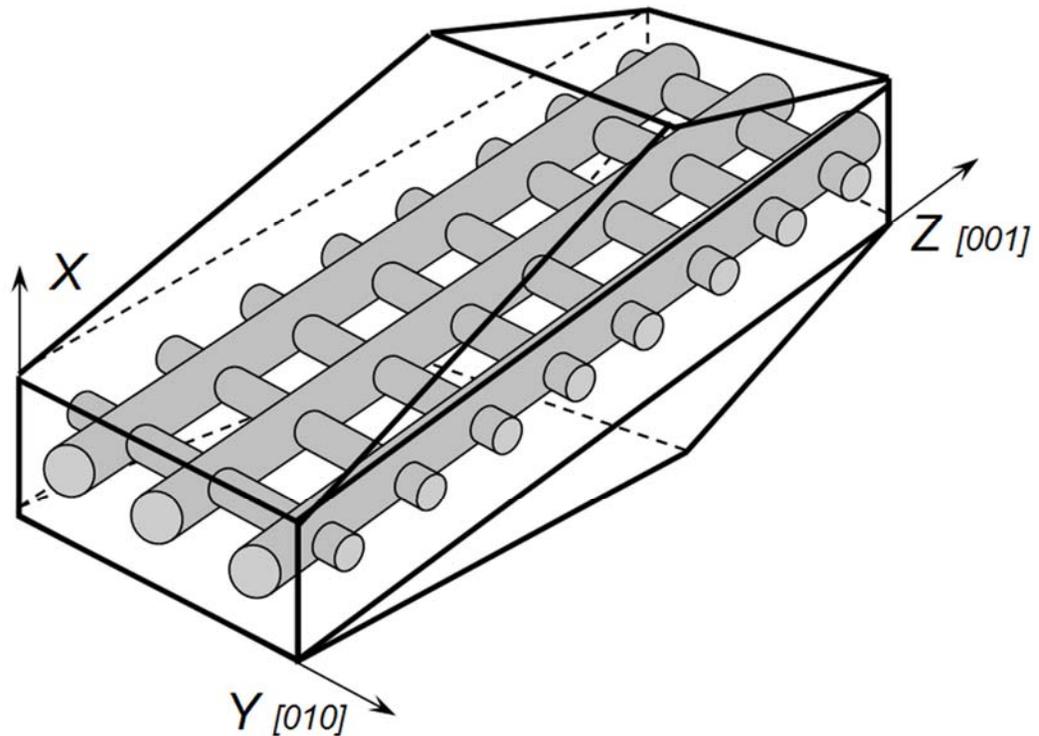
## 2-D pore structure of Ferrierite crystals



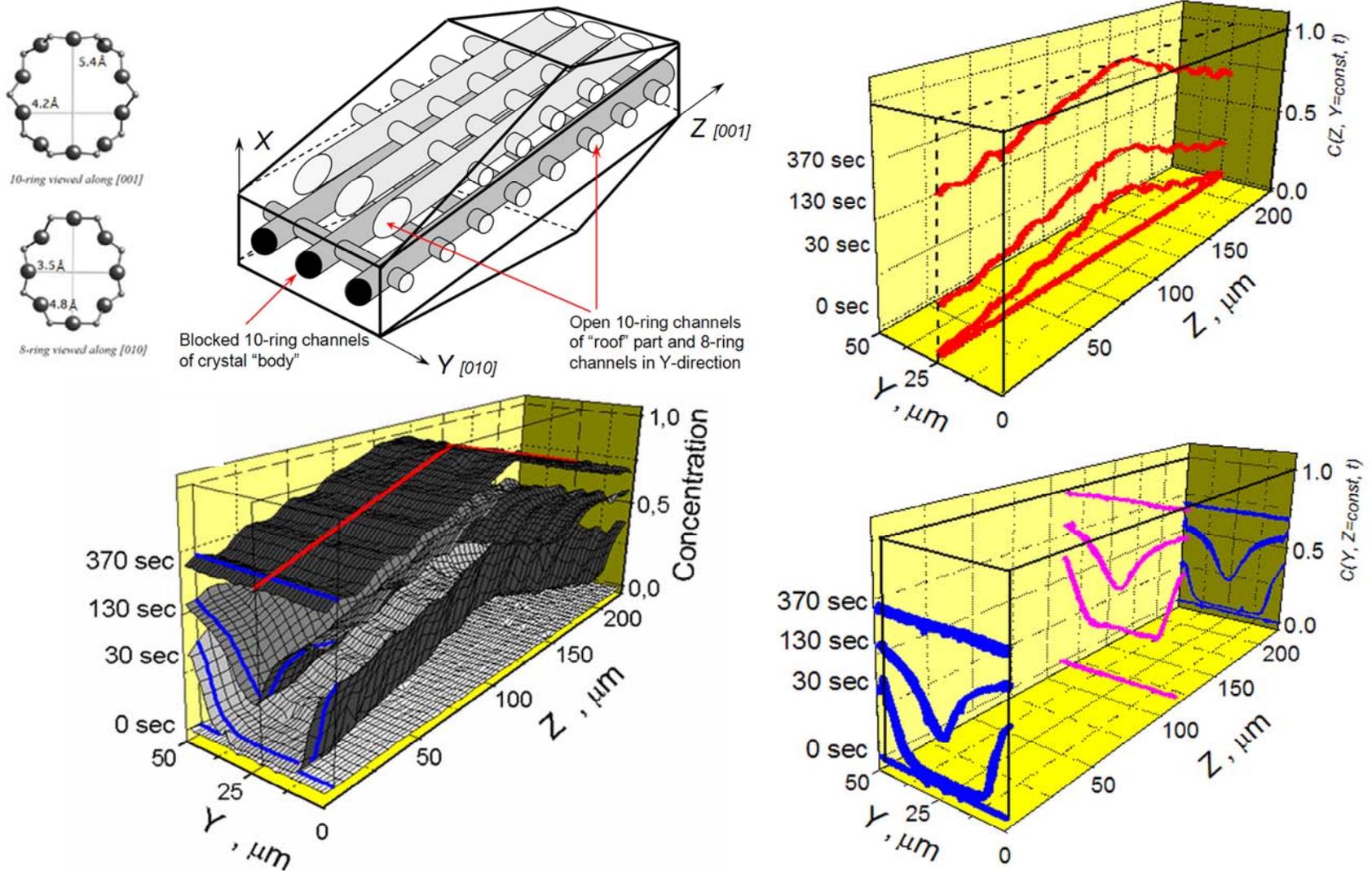
*10-ring viewed along [001]*



*8-ring viewed along [010]*

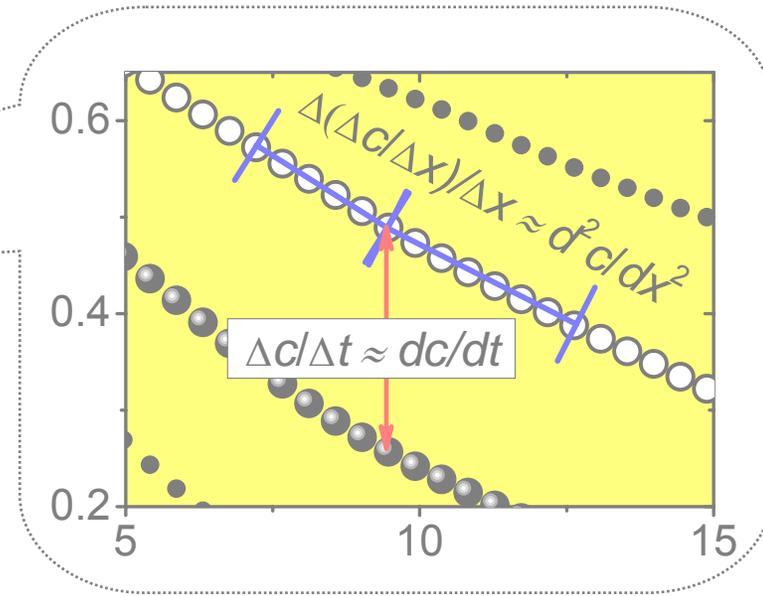
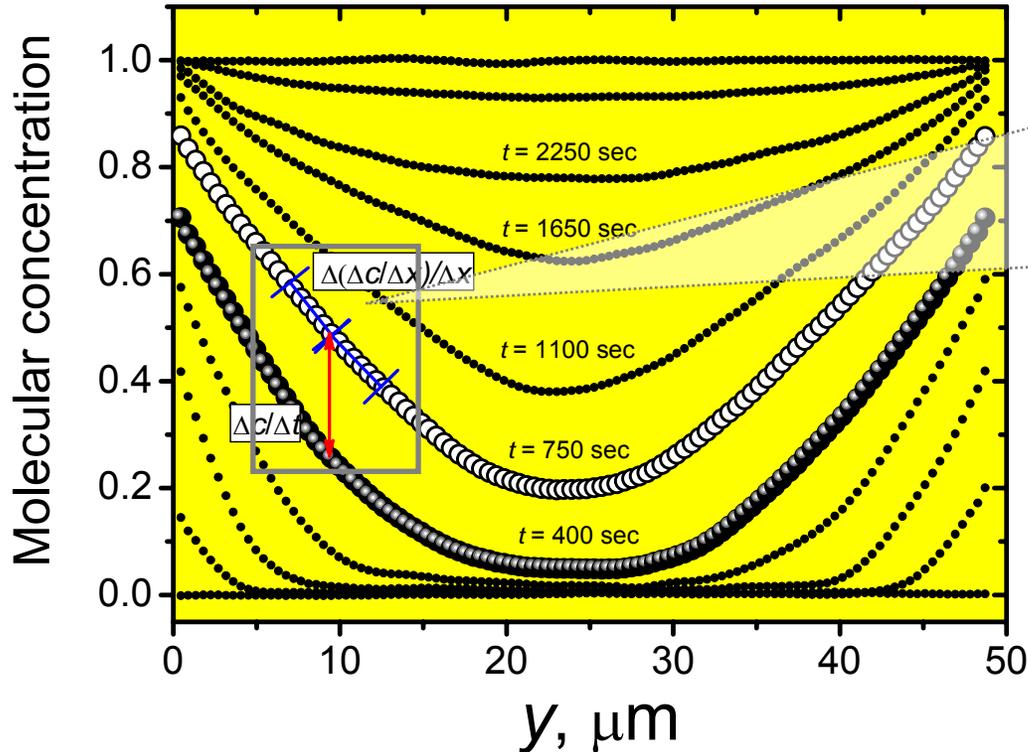


## Directions of methanol adsorption in Ferrierite crystal



## Local diffusion and surface resistance

Adsorption of Methanol (0 → 5 mbar) into Ferrierite



Fick's Second Law:

$x = 24 \mu\text{m}$

$$\frac{\partial c}{\partial t} = \frac{\partial}{\partial x} \left[ D(c, x) \frac{\partial c}{\partial x} \right] = \cancel{D(c, x)} \frac{\partial^2 c}{\partial x^2} + \frac{\partial D(c, x)}{\partial c} \cdot \left( \frac{\partial c}{\partial x} \right)^2$$

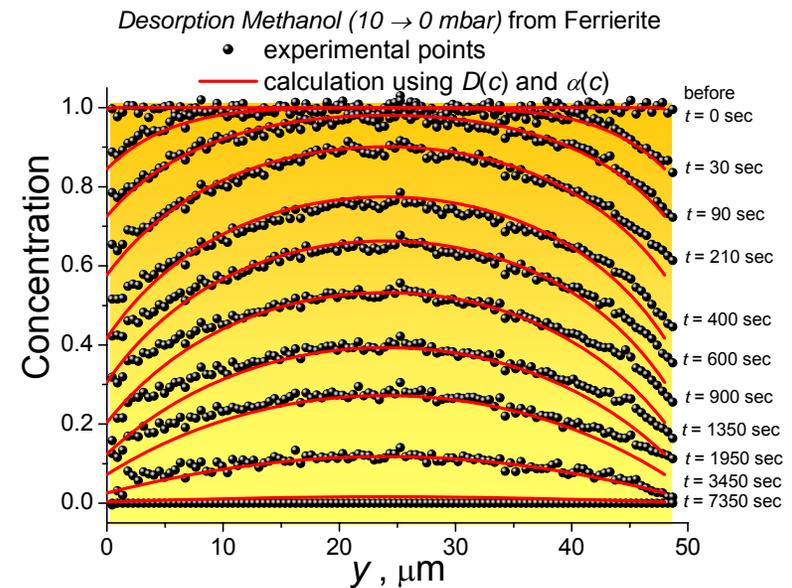
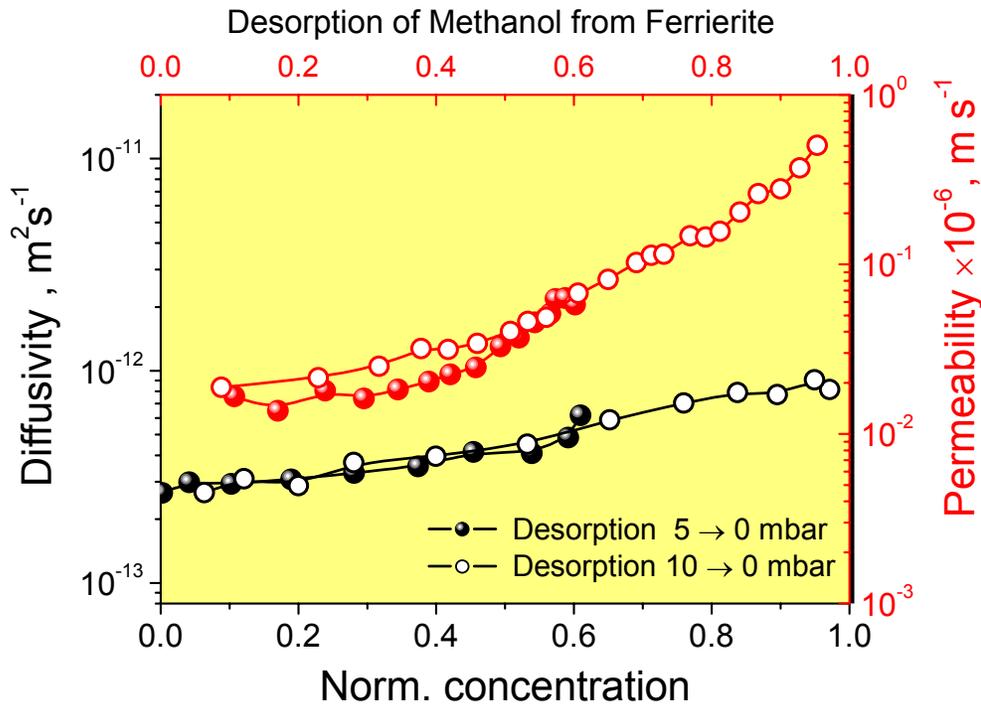
Fick's First Law:

$$j = \alpha (c_{eq} - c(t)) = D(c(t)) \cdot \frac{dc}{dx}$$

## Concentration dependence of the molecular diffusivity

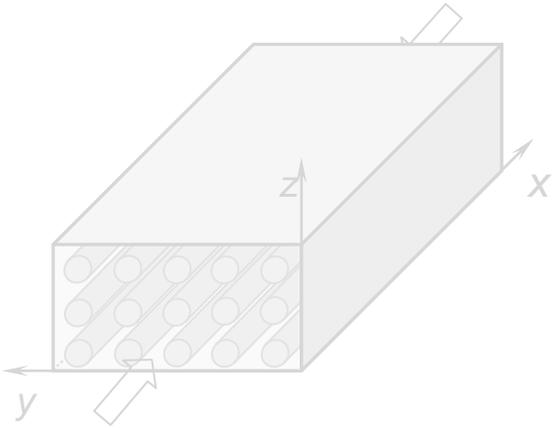
### Local DIFFUSION

### TEST

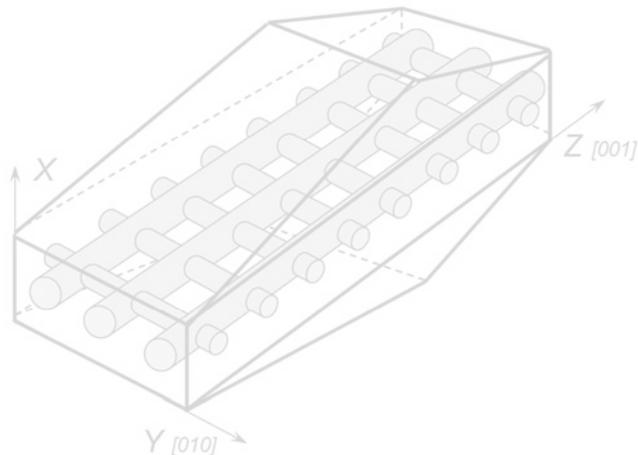


# Outline

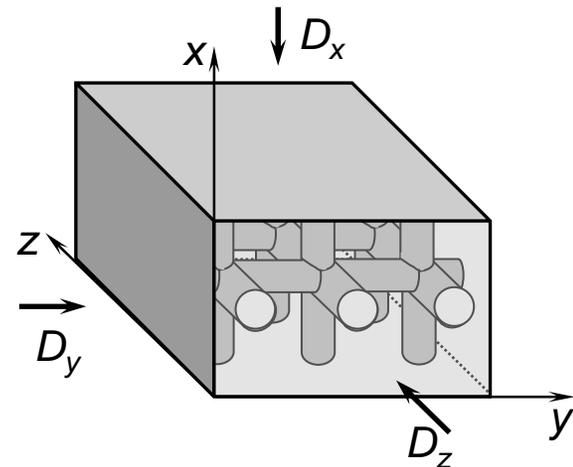
(a) 1-D pore structure of the MOF crystals



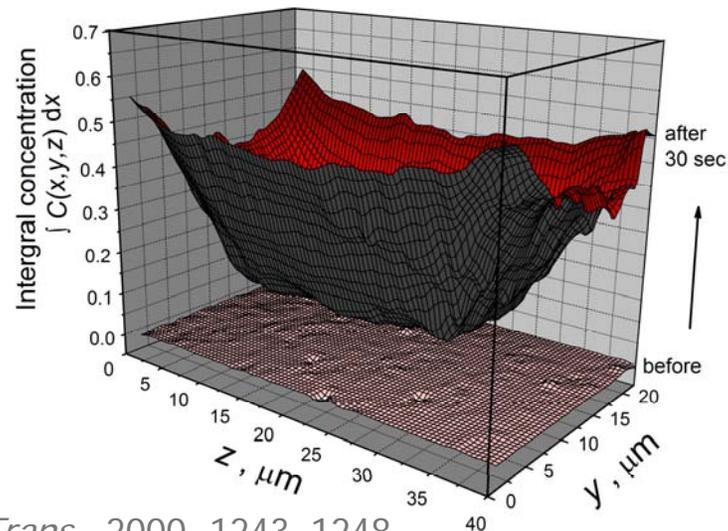
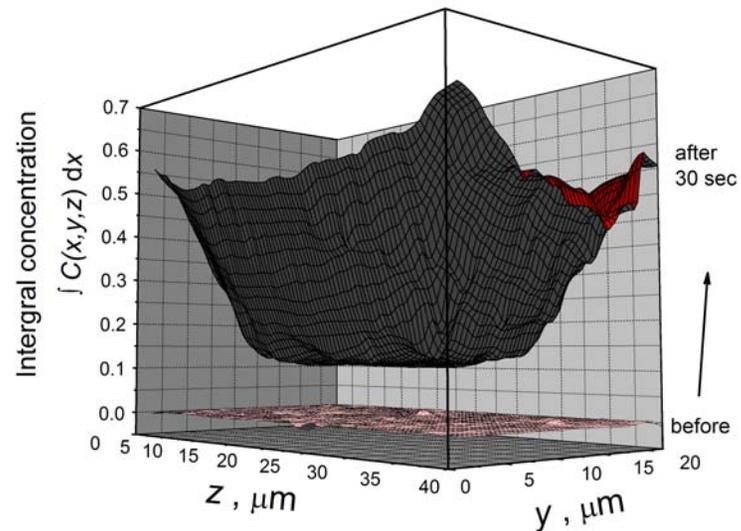
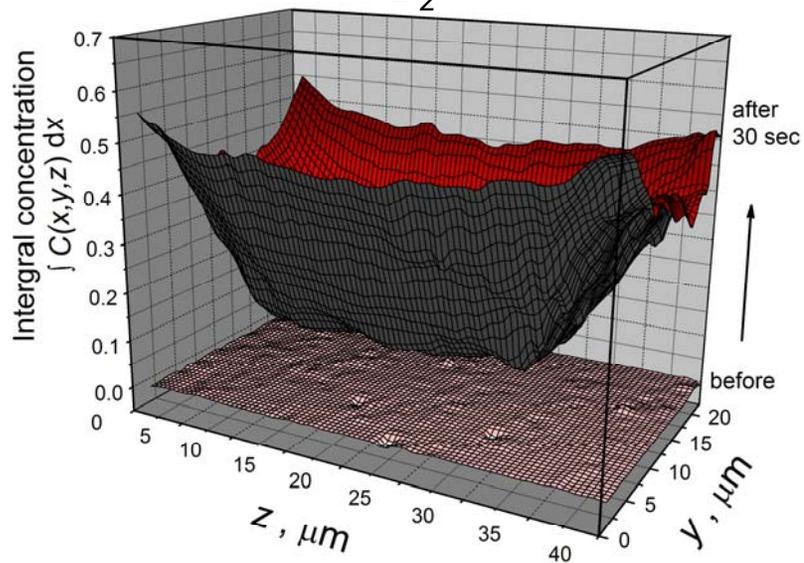
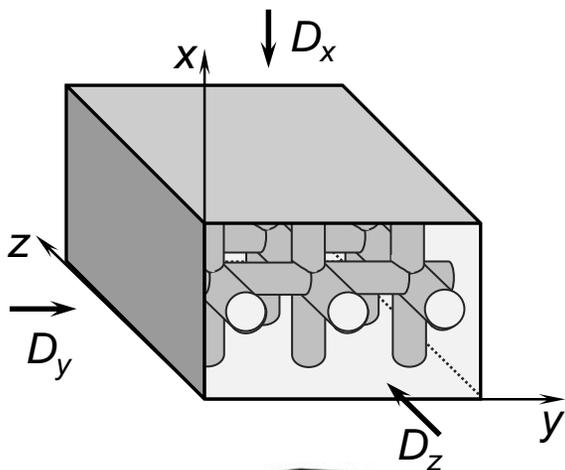
(b) 2-D pore structure of the Ferrierite zeolite



(c) 3-D pore structure of the SAPO STA-7

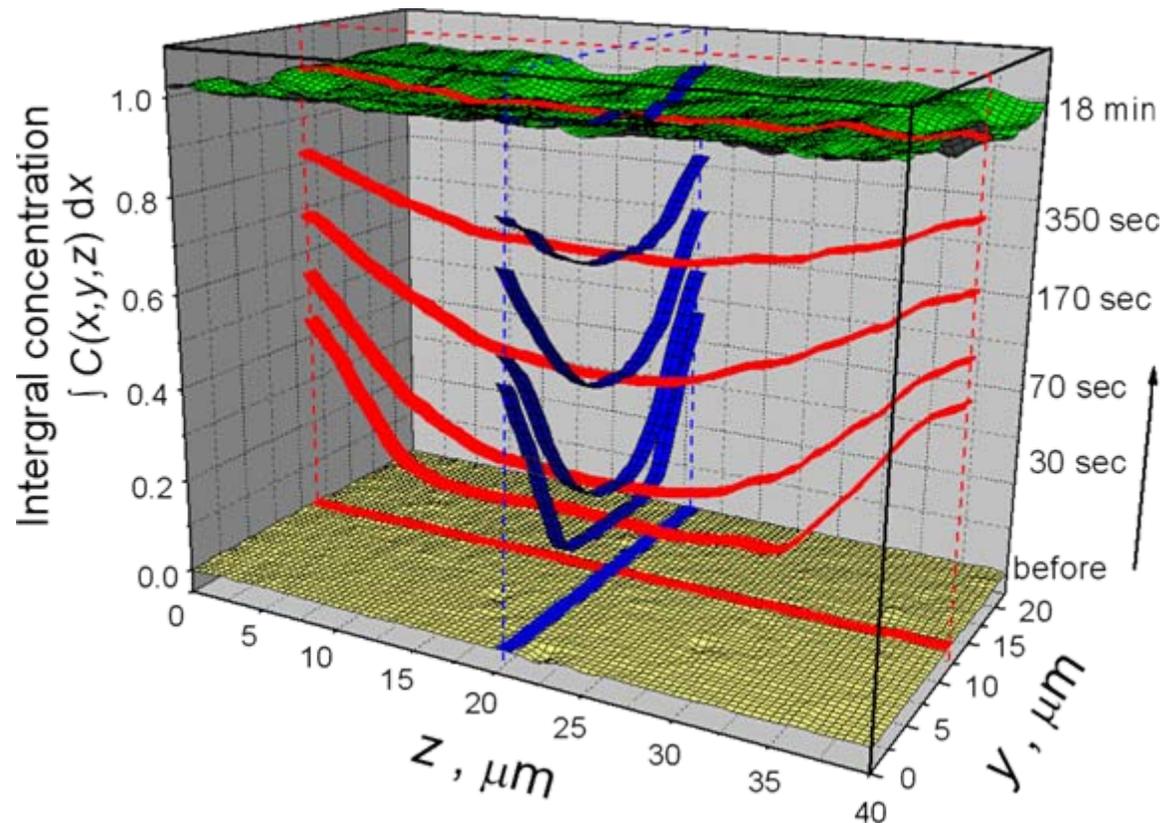
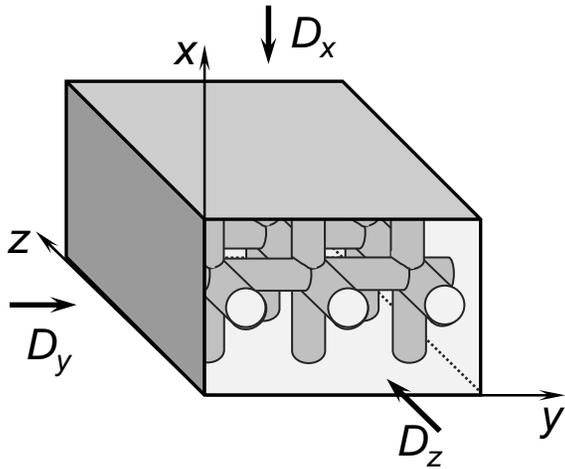


## 3-D pore structure of STA-7 materials (\*)

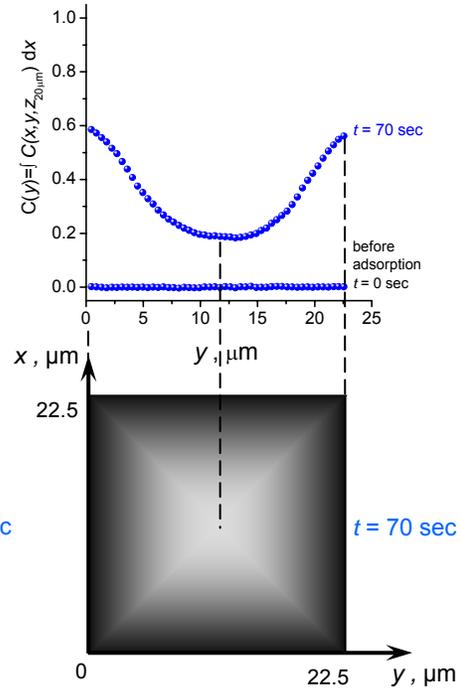
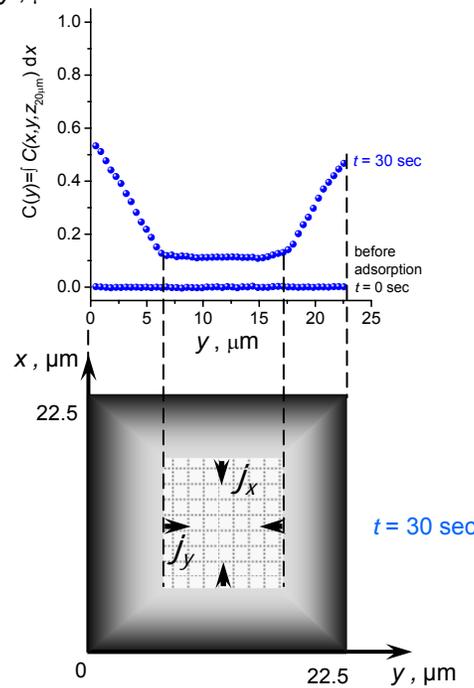
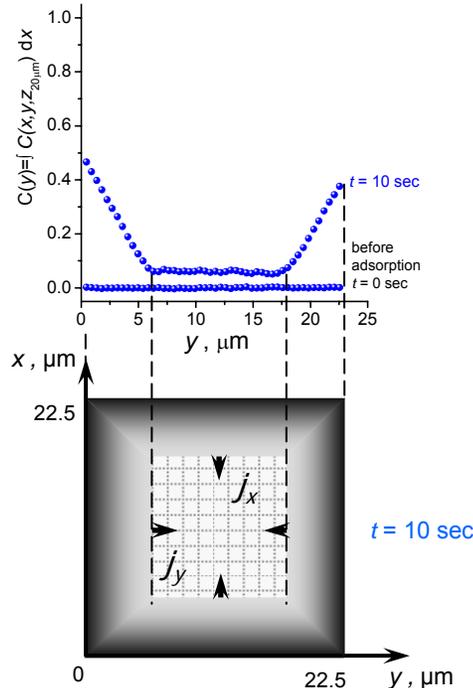
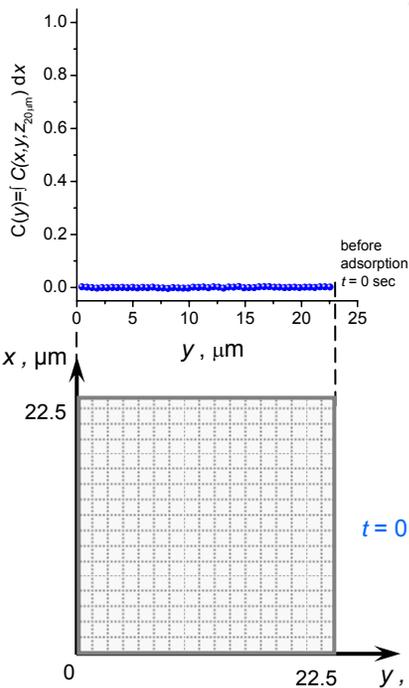
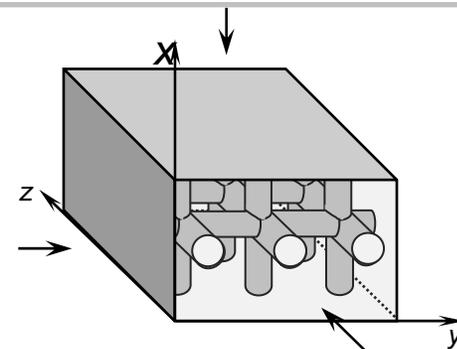
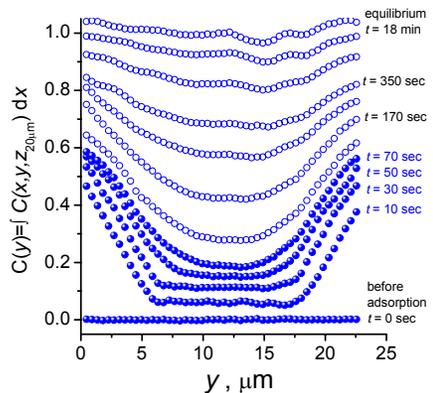
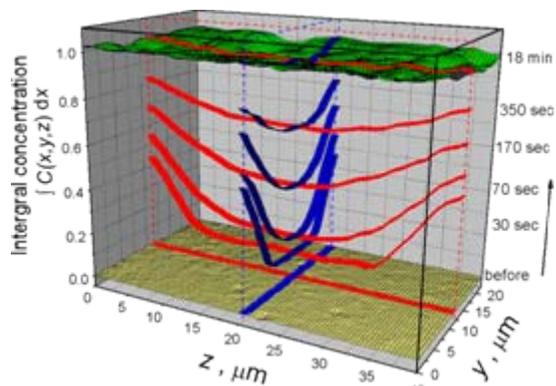


(\*) Paul A. Wright, Martin J. Maple et al., *J. Chem. Soc., Dalton Trans.*, 2000, 1243–1248

## 3-D pore structure of STA-7 materials



## Uptake in $y$ - and $x$ -directions



# IFM perspectives...

